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## **CLAIMS:**

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- 1. A method of secret key agreement between a first (16) and a second (18) correspondent, the method comprising the acts of:
  - (a) said first correspondent receiving a response A, from a source P (20);
- (b) said second correspondent receiving a response B from said source P (20);
- (c) said first correspondent generating (d-1) parity symbols as an output of a codeword W whose input includes said response A and a secret key K selected by said first correspondent (16);
- (d) said first correspondent (16) transmitting said (d-1) parity symbols over a public communication channel (22) to said second correspondent (18); and
- (e) said second correspondent (18) generating a word W' whose input includes said (d-1) parity symbols and said response B to determine said secret key K.
- 2. The method of Claim 1, wherein said responses A and B are received by said respective first (16) and second (18) correspondents responsive to a challenge C generated from said respective first (16) and second (18) correspondents.
- 3. The method of Claim 1, wherein said response A is comprised of a sequence of symbols of the form A=(a<sub>1</sub>,.....a<sub>n</sub>).
  - 4. The method of Claim 1, wherein said response B is comprised of a sequence of symbols of the form B=(b1,....,bn).
  - 5. The method of Claim 1, wherein said secret key K is comprised of a sequence of symbols of the form  $K=(k_1,\ldots,k_k)$ .
- 6. The method of Claim 1, wherein the secret key K may be determined from said (d-1) parity symbols and said response B by satisfying an inequality,

$$d_H(A,B) < = (d-1-k)/2$$

where d<sub>H</sub>(A,B) is the Hamming distance between symbol sequences A and B, d is the minimum distance, and k is the number of symbols in the secret key K.

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- 7. The method of Claim 1, wherein the codeword W is a Reed-Solomon codeword.
- 8. The method of Claim 1, wherein the secret key K cannot be determined by someone other than said first and second correspondent (18) if the following inequality is satisfied,

$$d_{H}(A,E) >= d-1$$

where:

E is a symbol sequence obtained by an attacker (17) attempting to learn

15 the secret key K,

d<sub>H</sub>(A,E) is the Hamming distance between the symbol sequences A and E,

and

d is the minimum distance.

9. A method of secret key agreement between a first and a second correspondent (18), the method comprising the acts of:

during an enrollment phase:

- (a) sending to a source (20), a challenge C, from a first correspondent (16) at a time t1;
- 25 (b) said first correspondent (16) receiving said response A to said challenge C;
  - (c) sending to said source (20), said challenge, from said second correspondent (18) B at a time t2;
- (d) said second correspondent (18) receiving a response B to said challenge C.

during an encoding phase, said first correspondent (16):

- (a) selecting a secret key K;
- (b) forming a codeword W using said secret key K and said response A to generate (d-1) parity symbols P;
- (c) transmitting said (d-1) parity symbols P to said second correspondent (18) over a public communication channel;

during a decoding phase, said second correspondent (18):

- (a) using said d-1 transmitted parity symbols and said response B to construct a word W' to determine the secret key K.
- 10 10. The method of Claim 9, wherein said response A is comprised of a sequence of symbols of the form  $A=(a_1,\ldots,a_n)$ .

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codeword.

- 11. The method of Claim 9, wherein said response B is comprised of a sequence of symbols of the form  $B=(b_1,\ldots,b_n)$ .
- 12. The method of Claim 9, wherein said secret key K is comprised of a sequence of symbols of the form  $K=(k_1,\ldots,k_k)$ .
- 13. The method of Claim 9, wherein the secret key K may be determined from 20 said word W' if and only if the inequality is satisfied

$$d_H(A,B) < = (d-1-k)/2$$

- where d<sub>H</sub>(A,B) is the Hamming distance between symbol sequences A and B, d is the minimum distance, and k is the number of symbols in the secret key K.
- 14. The method of Claim 9, wherein the codeword W is a Reed-Solomon

15. The method of Claim 9, wherein the secret key K cannot be determined from someone other than said first and second correspondent (18) if and only if the following inequality is satisfied:

$$d_{H}(A,E) >= d-1$$

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where E is a symbol sequence obtained by an attacker (17) attempting to learn the secret key K,

d<sub>H</sub>(A,E) is the Hamming distance between the symbol sequences A and E,

and

d is the minimum distance.

16. A method of secret key agreement between a first and a second correspondent (18), the method comprising the acts of:

said first correspondent (16) receiving a response A from a source P (20); said second correspondent (18) receiving a response B from said source P (20);

said first correspondent (16) generating (d-1) parity symbols as an output of a codeword W whose input includes said response A and a secret key K selected by said first correspondent (16);

said first correspondent (16) transmitting said (d-1) parity symbols and a pseudo-random function evaluated in A, over a public communication channel to said second correspondent (18); and

said second correspondent (18) generating a word W' whose input includes said (d-1) parity symbols, said pseudo-random function evaluated A, and said response B, to determine said secret key K selected by said first correspondent (16).

17. The method of Claim 16, wherein the pseudo-random function is a hash function of the form h(A)=(h(a1),...,h(an)), where A is the response A from said source P (20).

18. The method of Claim 16, wherein said response A is comprised of a sequence of symbols of the form  $A=(a_1,\ldots,a_n)$ .

- 19. The method of Claim 16, wherein said response B is comprised of a sequence of symbols of the form B=(b<sub>1</sub>,....,b<sub>n</sub>).
  - . 20. The method of Claim 16, wherein said secret key K is comprised of a sequence of symbols of the form  $K=(k_1,\ldots,k_k)$ .
- 10 21. The method of Claim 16, wherein the secret key K may be determined from said word W' if the inequality is satisfied,

$$d_H(A,B) < = (d-1-k)$$

where d<sub>H</sub>(A,B) is the Hamming distance between symbol sequences A and B,
d is the minimum distance, and
k is the number of symbols in the secret key K.

- 22. The method of Claim 16, wherein the codeword W is a Reed-Solomon codeword.
- 23. The method of Claim 16, wherein the secret key K cannot be determined from someone other than said first and second correspondent (18)s if the following inequality is satisfied:

$$d_{H}(A,E) >= d-1$$

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where E is an attacker (17) attempting to learn the secret key K,  $d_H(A,E) \text{ is the Hamming distance between the symbol sequences A and E,}$  and

d is the minimum distance.

24. A method of secret key agreement between a first and a second correspondent (18), the method comprising the acts of:

during an enrollment phase:

sending to a source (20), a challenge C, from said first

5 correspondent (16) at a time t1;

receiving said response A to said challenge C;

sending to said source (20), said challenge C, from said second correspondent (18) at a time t2;

during an encoding phase:

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said first correspondent (16) selecting a secret key K; forming a codeword W using said secret key K, a response A

received by said first correspondent (16) during an enrollment phase and d-1 parity symbols P;

transmitting said d-1 parity symbols P and h(A) a pseudo-random function of A from said first correspondent (16) to said second correspondent (18) over a public communication channel;

during a decoding phase:

using said d-1 transmitted parity symbols and said pseudo-random function evaluated in A by said second correspondent (18) to construct a word W' to determine the secret key K.

- 25. The method of Claim 24, wherein the pseudo-random function is a hash function  $h(A)=(h(a_1),...,h(a_n))$
- 25 26. The method of Claim 24, wherein said response A is comprised of a sequence of symbols of the form  $A=(a_1,\ldots,a_n)$ .
  - 27. The method of Claim 24, wherein said response B is comprised of a sequence of symbols of the form  $B=(b_1,\ldots,b_n)$ .

. 28. The method of Claim 24, wherein said secret key K is comprised of a sequence of symbols of the form  $K=(k_1,\ldots,k_k)$ .

29. The method of Claim 24, wherein the secret key K may be determined from said word W' if the inequality is satisfied,

$$d_H(A,B) < = (d-1-k)$$

where d<sub>H</sub>(A,B) is the Hamming distance between symbol sequences A and B, d is the minimum distance, and k is the number of symbols in the secret key K.

- 30. The method of Claim 24, wherein the codeword W is a Reed-Solomon codeword.
- 15 31. The method of Claim 24, wherein the secret key K cannot be determined from someone other than said first and second correspondents (16,18) if the following inequality is satisfied:

$$d_{H}(A,E) >= d-1$$

20 where E is a symbol sequence obtained by an attacker (17) attempting to learn the secret key K,

d<sub>H</sub>(A,E) is the Hamming distance between the symbol sequences A and E,

d is the minimum distance.

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and

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32. A method of secret key agreement between a first and a second correspondent (18), the method comprising the acts of:

said first correspondent (16) receiving a response A from a source P (20), where A is a set of symbols;

said second correspondent (18) receiving a response B from said source P (20), where B is a set of symbols;

. .......

said first correspondent (16) ordering the set of symbols A into a sequence,  $a_1, \ldots, a_N$ ;

said first correspondent (16) computing a pseudo-random function of the ordered set of symbols A, h(A);

said first correspondent (16) transmitting h(A)=(h(a1),...h(an)) to said second correspondent (18); and;

said second correspondent (18) computing a pseudo-random function of the ordered set of symbols B, h(b) for each symbol b in the set B;

said second correspondent (18) computing a set S which includes all positions j for which there exists an element in B such that  $h(a_i) = h(b)$ ;

said second correspondent (18) transmitting the set S back to said first correspondent (16); and

both first and second correspondents (16, 18) extracting a joint key J based on the symbols  $a_j$ , j in S and for those symbols b in set B for which  $h(a_j) = h(b)$ .

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- 33. The method of Claim 32, further comprising the act of extracting a secret key K from said joint key J using privacy amplification.
- 34. The method of Claim 33, wherein using said privacy amplification includes using one of a random matrix multiplier for multiplication with the joint key J and the joint key J evaluated in a hash function.
  - 35. The method of Claim 32, wherein said responses A and B are received by said respective first (16) and second (18) correspondents responsive to a challenge C generated from said respective first (16) and second (18) correspondents.
  - 36. The method of Claim 32, wherein said response A is comprised of a sequence of symbols of the form  $A=(a_1,\ldots,a_n)$ .
- 37. The method of Claim 32, wherein said response B is comprised of a sequence of symbols of the form  $B=(b_1,\ldots,b_n)$ .

. 38. The method of Claim 32, wherein said secret key K is comprised of a sequence of symbols of the form  $K=(k_1,\ldots,k_k)$ .